

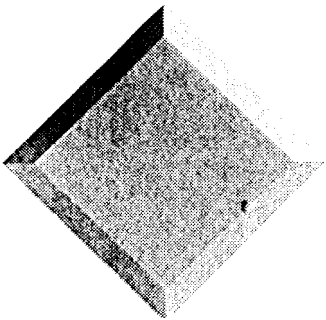
## Finding Fault with Faults: A Case Study

Allen P. Nikora  
Jet Propulsion Laboratory  
4800 Oak Grove Drive  
Pasadena, CA 91109-8099  
Mail Stop 264-805  
vox: (818)393-1104  
fax: (818)393-7830  
Allen. P. Nikora@jpl.nasa.gov

John C. Munson  
Computer Science Department  
University of Idaho  
Moscow, ID 83844-1010  
vox: (208)885-7789  
fax: (208)885-9052  
jmunson@cs.uidaho.edu

### ABSTRACT

Over the past several years, **significant** effort has been devoted to the process of predicting **software** system fault content during the earlier development phases. Much of this work has **involved** relating structural characteristics of software systems (e.g. complexity measurements of the source code and design) to the number of **faults** in the system. We describe our **effort** in extending this work beyond the initial **software** construction. Our area offocus is determining the rate offault injection over a sequence of successive builds, **first** observing that **software** faults may be seen to fall into two distinct classes - some faults are incorporated during the initial coding **effort**, while others are added in successive **software** builds. Experience in working **with** NASA **software** development efforts is discussed, including practical issues in obtaining data and assuring its validity. One of the most **significant** topics discussed is the methodology for the precise determination of a **fault** condition and the mapping of **software** faults to individual program modules. We examine the results obtained to date, and conclude **with** a description of our plans to extend this work in the future.



# ***FINDING FAULT WITH FAULTS. A CASE STUDY***

**Allen P. Nikora**

**Jet Propulsion Laboratory**

**California Institute of Technology**

**Pasadena, CA**

**Allen.P.Nikora@jpl.nasa.gov**

**John C. Munson**

**Computer Science Department**

**University of Idaho**

**Moscow, ID**

**jmunson@cs.uidaho.edu**

**Annual Oregon Workshops on Software Metrics**

**May 11-13, 1997**

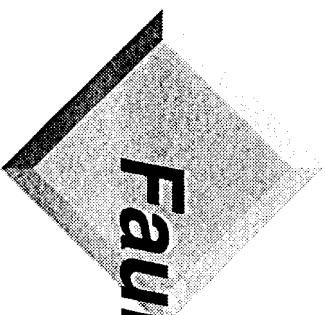
**Coeur d'Alene, ID**

# Overview

- ❖ Motivation
- ❖ Fault Content Model
- ❖ Counting Faults
- ❖ Fault surrogates
- ❖ Rate of fault injection
- ❖ Risk Assessment
- ❖ Future Work

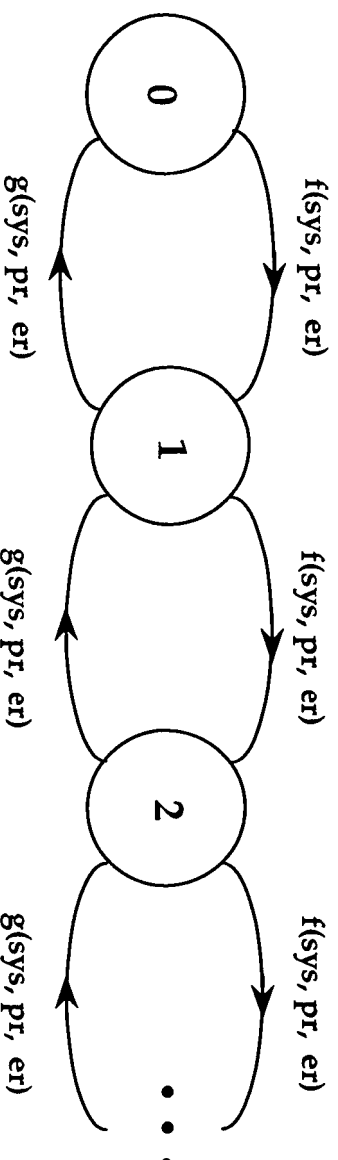


- ❖ Current methods of predicting software reliability don't account for system's structure and development process characteristics.
- ❖ To manage better a development effort, must be able to trade off between development process options, system structure options, and quality while development still in progress.
- ❖ Goals:
  - ❖ Develop improved methods of measuring a software system to assess operational risk
  - ❖ Assert better control over the system structure and the development process using these improved measures



# Fault Content Model

## General Model Formulation

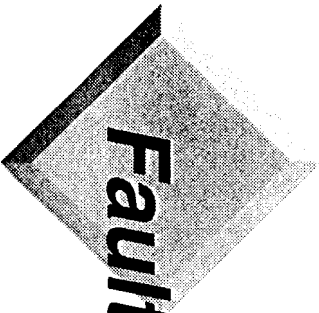


**$f$  and  $g$  are functions:**

$\text{sys}$  represents characteristics of the software product

$\text{pr}$  represents characteristics of the software development process

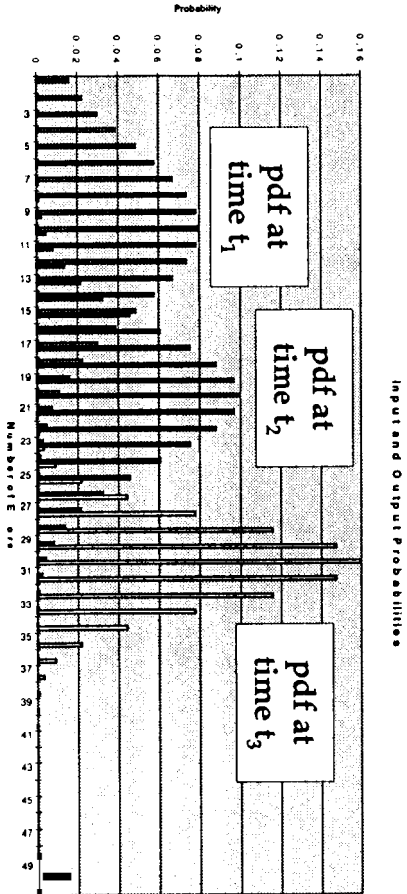
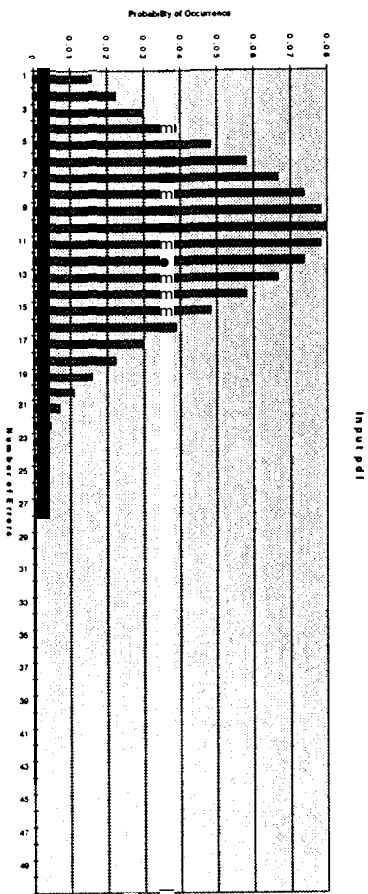
$\text{er}$  represents the number of faults already in the system

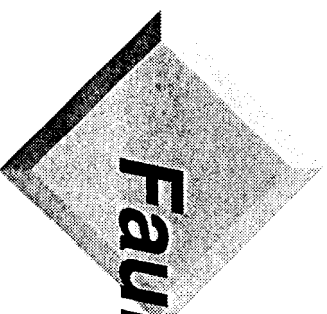


# Fault Content Model (cont'd)

## General Model Formulation (cont'd):

- Input:  $\equiv$
- Output:  $\equiv$



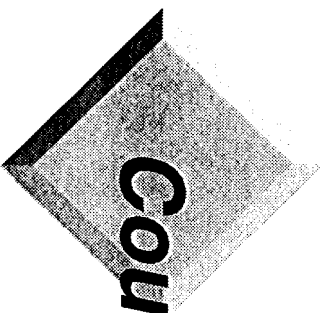


## ***Fault Content Model (cont'd)***

### **Advantages of the new model:**

- Ability to make resource/risk tradeoffs earlier in the development effort.
- Ability to refine and update predictions as more detailed information about product, risk, and process becomes available.
- Ability to compute confidence values.
- Predictions are in terms meaningful to users and developers.

**Development and use of model requires the ability to consistently accurately faults.**



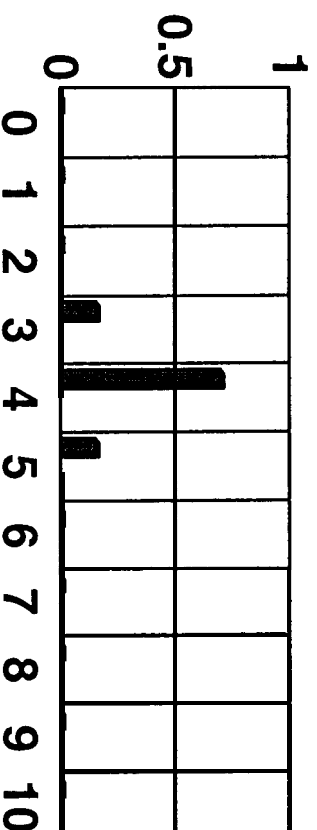
# ***Counting Faults***

- ❖ **Fault vs. Failure counts**
- ❖ **Post-development Fault Identification**
- ❖ **Fault Types**
- ❖ **Fault Type Composition**

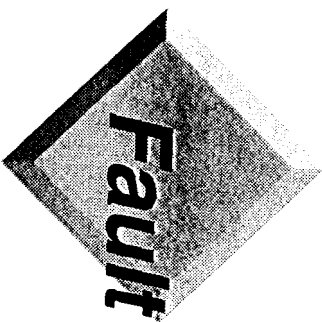


## ***Fault vs. Failure Counts***

- ❖ **Failure counts could be used if:**
  - ❖ **Number of faults related to number of failures**
  - ❖ **Distribution of number of faults per failure had low variance**

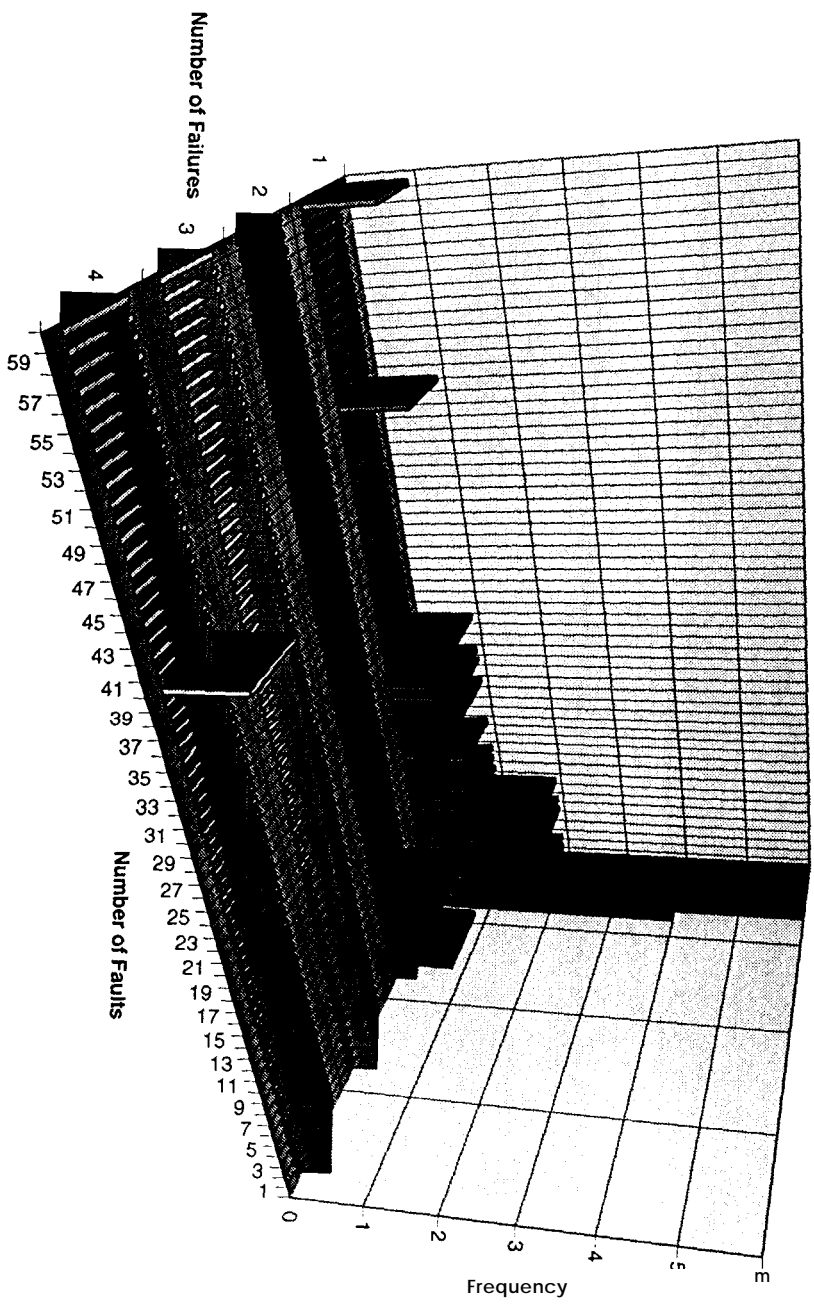


- ❖ **Actual situation is shown on next slide**



# Fault vs. Failure Counts (cont'd)

D      0      Faults per Failure





# ***Counting Faults - Post-Development Identification***

- ❖ **Available data**
  - ❖ Institutional problem reporting systems
  - ❖ SCCS files for all delivered versions of software
- ❖ **Identifying faults**
  - ❖ Model repairer is increment “x” in response to a failure
  - ❖ Assume changes in increment but “x” due solely to fault repair
  - ❖ Difference between “x-1” and “x” identifies changes (faults)
  - ❖ Look for earliest increments in which faults occur

**Post-development fault identification is primarily a**

**manual process**



# ***Fault Types***

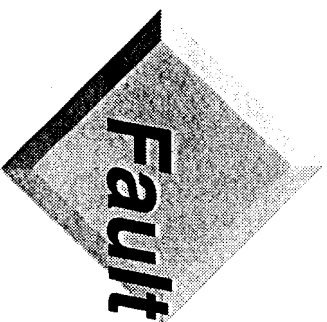
**Taxonomy based on corrective actions taken in response to failure reports**

- ❖ **Faults is variable usage**
  - ❖ **Definition and use of new variables**
  - ❖ **Redefinition of existing variables (e.g. changing type from float to double)**
  - ❖ **Variable deletion**
  - ❖ **Assignment of a different value to a variable**
- ❖ **Faults involving constants**
  - ❖ **Definition and use of new constants**
  - ❖ **Constant definition deletion**



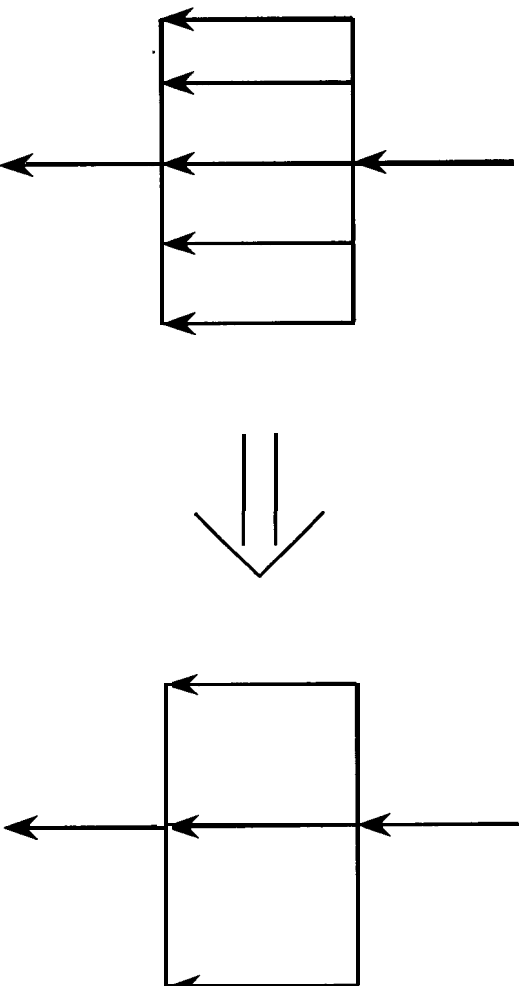
## ***Fault Types (cont'd)***

- ❖ **Control flow faults**
  - ❖ Addition of new source code block
  - ❖ Deletion of erroneous conditionally-executed path(s) within a source code block
  - ❖ Addition of execution paths within a source code block
  - ❖ Redefinition of condition for execution (e.g. change “if i < 9” to “if i <= 9”)
  - ❖ Removal of source code block
  - ❖ Incorrect order of execution
  - ❖ Addition of a procedure or function
  - ❖ Deletion of a procedure or function



## ***Fault Types (cont'd)***

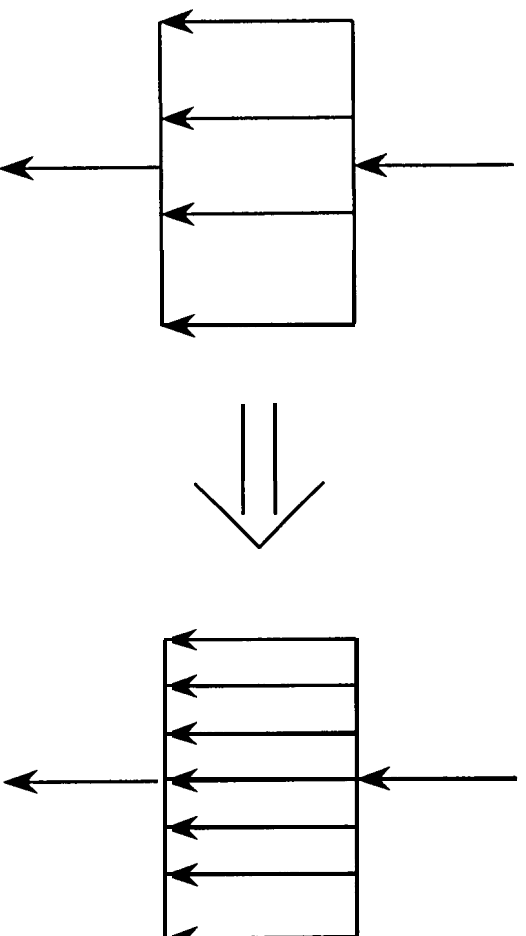
**Control flow fault examples - removing execution paths from a code block**



**Counts as two faults, since two paths were removed**

## ***Fault Types (cont'd)***

**Control flow examples (cont'd) - addition of conditional execution paths to code block**



**Counts as three faults, since three paths were added**



# ***The Introduction of Faults***

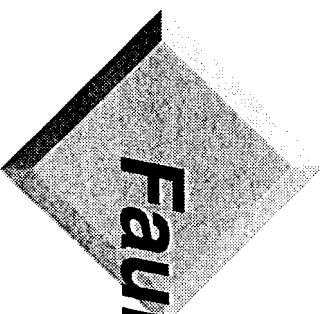
- ❖ People make errors in the interpretation of their tasks
    - ❖ System Analysts
    - ❖ Systems Designers
    - ❖ Programmers
  - ❖ These errors are manifested in
    - ❖ Specifications
    - ❖ Designs
    - ❖ Programs
- as faults**





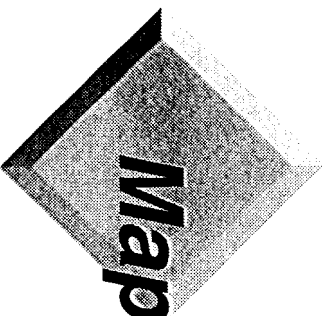
# ***Faults and Uncertainty***

- ❖ Can never know when all faults have been found
- ❖ May only use past experience to anticipate fault count in any reasonable manner
- ❖ We seek to develop a fault surrogate
  - ❖ Obtained estimate from past development efforts
  - ❖ Varies directly with faults
  - ❖ Anticipates distribution of faults in modules



## ***Fault Granularity***

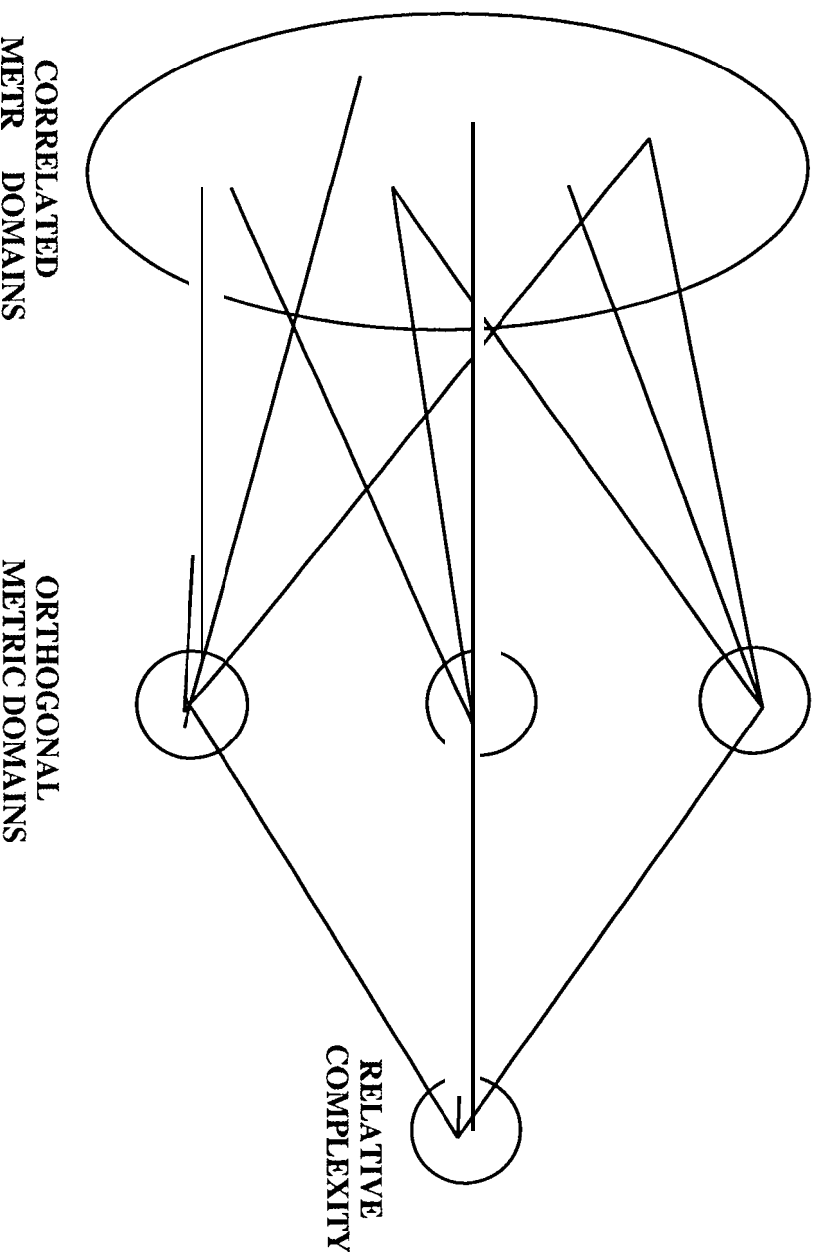
- ❖ The granularity of fault measurement must be the same as other metrics
- ❖ Changes to  $\infty$  are measured at the module level
- ❖ Complexity measurements are at the module level
- ❖ Configuration management is at the module level
- ❖ Faults should be maintained at the module level



## *Mapping of Faults*

- ❖ **One fault - one module**
  - ❖ **Fault extent within single module**
- ❖ **One fault - several modules**
  - ❖ **include problem**
  - ❖ **COMPOOLS**
  - ❖ **global data**

# *Deriving a Fault Surrogate From Complexity Metrics*



# ***Selection of Metrics for Fault Surrogate***

- ❖ Software metrics are highly correlated
- ❖ Selected for their relationship to faults
- ❖ Principal components analysis used to identify distinct sources of variation

❖ The ~~win~~ <sup>seen</sup> sixteen original metrics:

|       |     |      |     |     |     |     |     |     |
|-------|-----|------|-----|-----|-----|-----|-----|-----|
| • 49  | 295 | 1509 | 858 | 356 | 379 | 460 | 106 | 135 |
| 10000 | 16  | 179  | 159 | 48  | 14  | 17  | 12  | 32  |
| 5     | 54  | 2    | 45  | 5   |     |     |     |     |

❖ When standardized become:

|        |       |      |      |      |      |      |       |
|--------|-------|------|------|------|------|------|-------|
| • 3.15 | 1.73  | 0.97 | 0.68 | 2.38 | 1.04 | 1.44 | 1.60  |
| 1.47   | 2.42  | 5.64 | 3.78 | 3.70 | 2.10 | 1.13 | -1.10 |
| 1.32   | -0.52 | 1.41 |      |      |      |      |       |

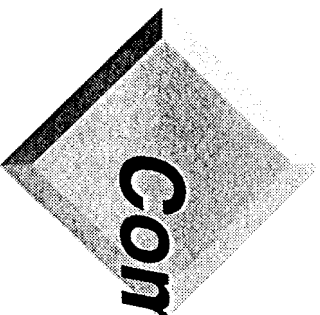
❖ Standardized metrics are transformed to become:

|        |      |      |       |
|--------|------|------|-------|
| • 3.84 | 0.89 | 0.54 | -0.18 |
|--------|------|------|-------|



# ***A Unitary Measure of Software Complexity***

- ❖ Each complexity domain has a distinct relationship with measure of faults
- ❖ Identify complexity domains that are closely related to software faults
- ❖ Compute domain metrics for each complexity domain so related
- ❖ Relative Complexity is a weighted sum of the domain metrics



## *Computation of Relative Complexity*

- ❖ For each program module, a set of measurements will be taken on selected metric primitive  $\mathcal{SS}$
- ❖ Transformation coefficients  $t_{jk}$  will map the standardized raw metrics  $z_{ij}$  onto a set of domain metrics (factor scores)
- ❖ A relative complexity value,  $\rho_i$ , will be computed for each program module as follows:

$$\rho_i = \sum_k \left( \sum_j z_{ij} t_{jk} \right) \lambda_k$$



## ***Relative Complexity As a Fault Surrogate***

- ❖ Program modules may be ordered by relative complexity
- ❖ The relative complexity of a software system is the average relative complexity of the component modules
- ❖ Relative complexity is an extensible metric
- ❖ Validation of the relative complexity concept
  - ❖ Correlates well (0.90) with measures of software faults






## ***Relative Complexity As a Fault Surrogate***

- ❖ If the relative complexity of a module is high then it will contain a large number of faults
- ❖ The metrics that comprise relative complexity were selected because they were related to faults
- ❖ If the relative complexity of a module changes during development, then the number of latent faults will also change



# Sample Hal/S Programs Ordered by Relative Complexity

| Module | Domain1 | Domain2 | Domain3 | p      | DR Count |
|--------|---------|---------|---------|--------|----------|
| 1      | -0.78   | -0.01   | 0.36    | 43.36  | 0        |
| 2      | -0.77   | -0.02   | 0.36    | 43.37  | 0        |
| 3      | -0.77   | -0.02   | 0.35    | 43.37  | 0        |
| 4      | -0.77   | -0.02   | 0.34    | 43.39  | 0        |
| 5      | -0.76   | -0.03   | 0.34    | 43.40  | 0        |
| 6      | -0.76   | -0.00   | 0.31    | 43.53  | 0        |
| 7      | -0.76   | -0.00   | 0.31    | 43.53  | 0        |
| 8      | 3.16    | 3.27    | 2.55    | 95.44  | 9        |
| 9      | 7.57    | -5.39   | 1.66    | 97.84  | 25       |
| 10     | 3.75    | 3.19    | 1.31    | 98.80  | 4        |
| 11     | 3.45    | 4.46    | 3.06    | 103.64 | 6        |
| 12     | 4.82    | 2.45    | 0.26    | 104.02 | 4        |
| 13     | 5.98    | 3.08    | 6.09    | 124.72 | 10       |
| 14     | 8.24    | 5.13    | -0.86   | 144.42 | 15       |

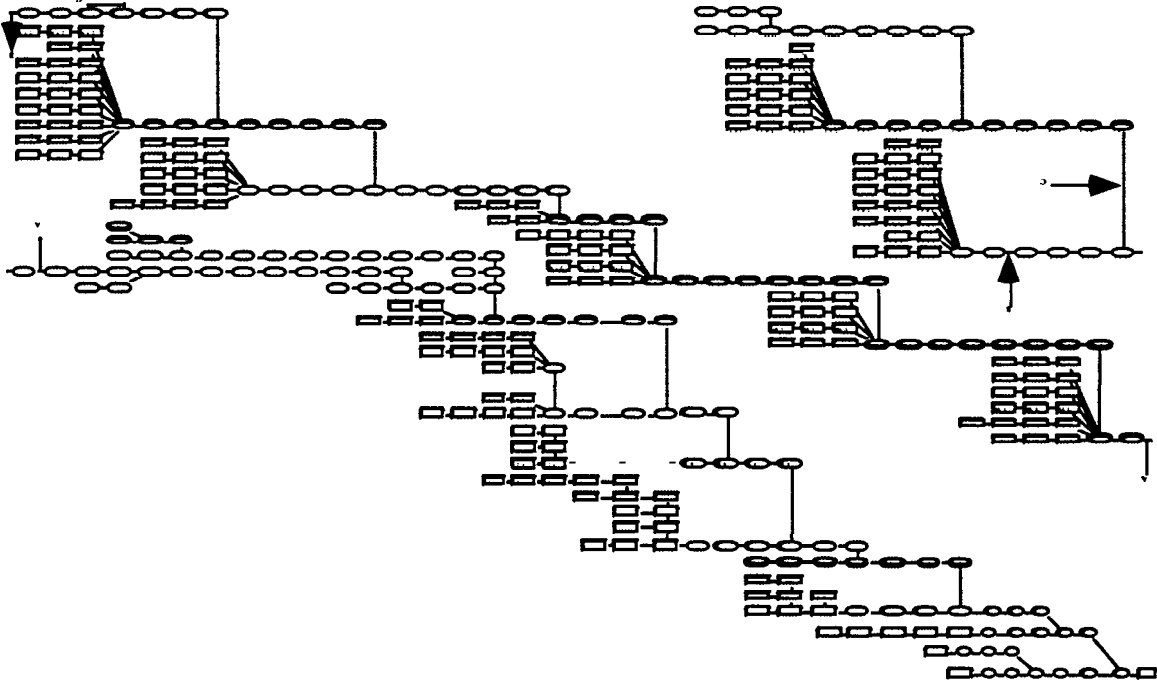


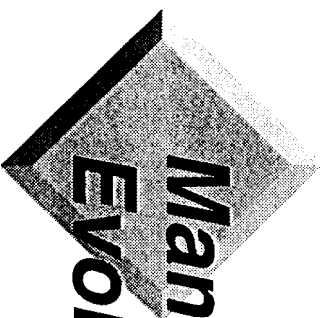
# **Software Evolution: Measuring a Moving Target**

- ❖ We assume that we are developing (maintaining) *a program*
- ❖ We are really working with many programs over time
- ❖ They are *different* programs in a very real sense
- ❖ We must identify and measure each version of each program module

# *The Evolution of the Space Shuttle*

**Pass**





# ***Managing Fault Counts During Evolution***

- ❖ **Some faults are inserted during branch builds**
  - ❖ **These fault counts must be removed when the branch is pruned**
- ❖ **Some faults are eliminated on branch builds**
  - ❖ **These faults must be removed from the main sequence build**
- ❖ **Fault count should contain only those faults on the main sequence to the current build**
- ❖ **Faults attributed to modules not in the current build must be removed from the current count**



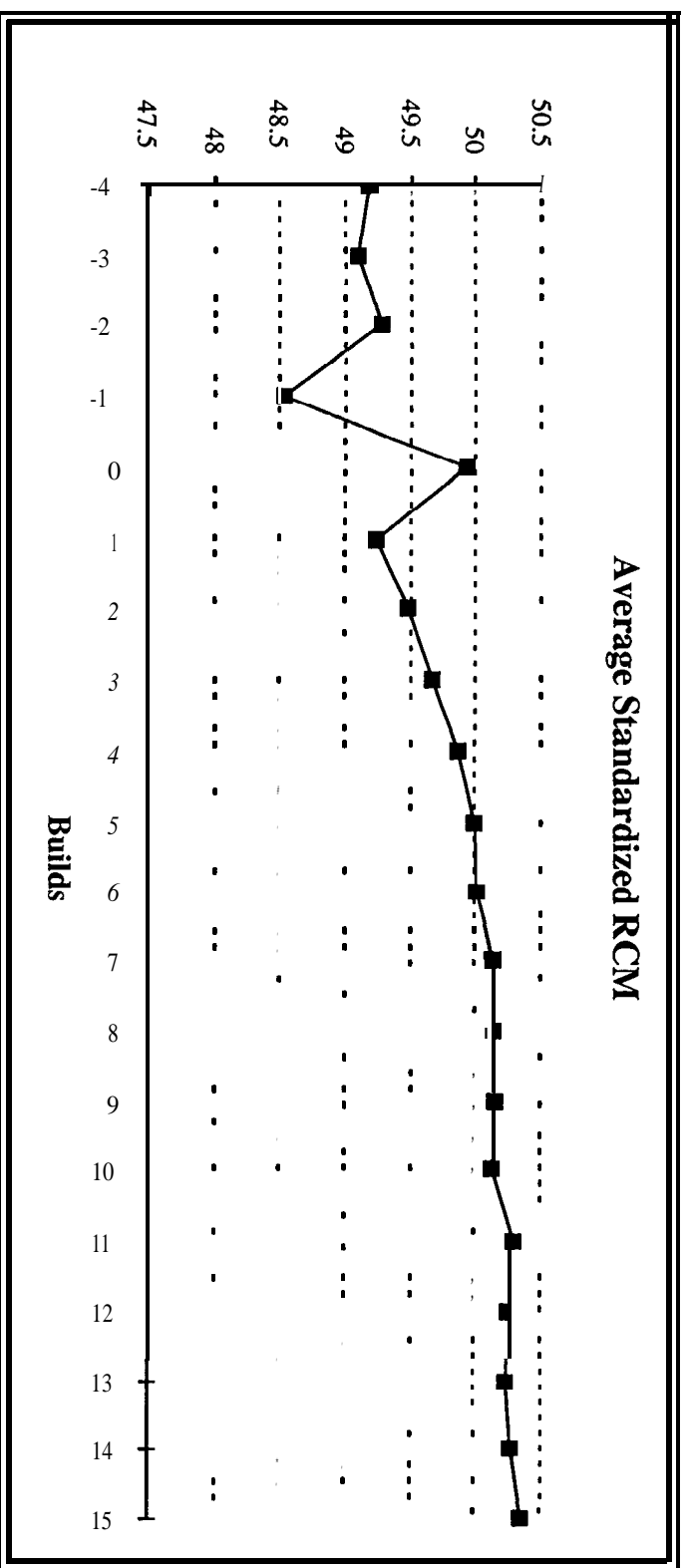
# ***Baselining a Software Development Project***

- ❖ **Software changes over software builds**
- ❖ **Measurements, such as relative complexity, change across builds**
- ❖ **Initial build as a *baseline***
- ❖ **Relative complexity of each build**
- ❖ **Measure change in fault surrogate from initial baseline**

# ***Change As a Fault Injection Process***

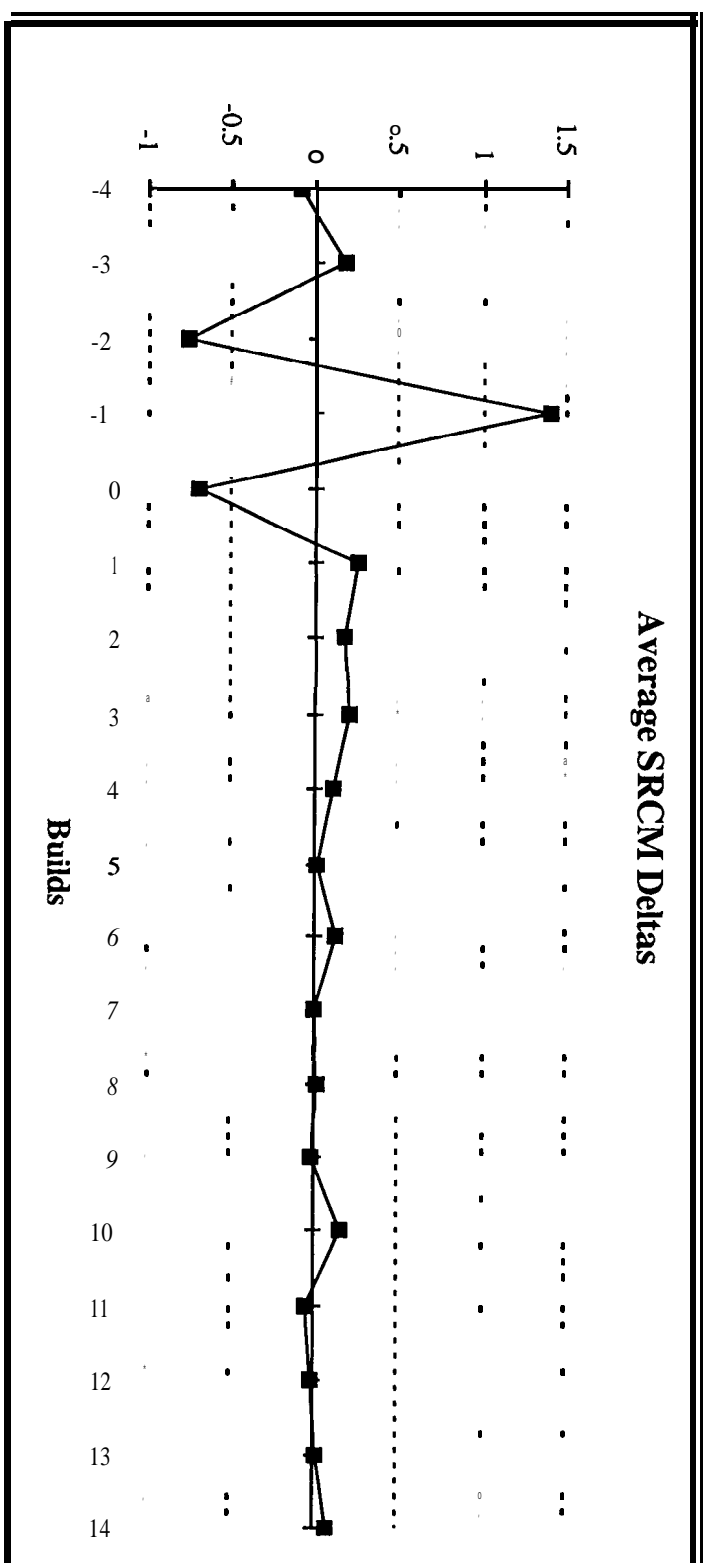
- ❖ New faults are introduced with system changes
- ❖ Number of faults is proportional to degree of change
- ❖ Domain complexities are measures of specific changes
- ❖ Relative complexity is a measure of change
- ❖ Relative complexity is a fault surrogate

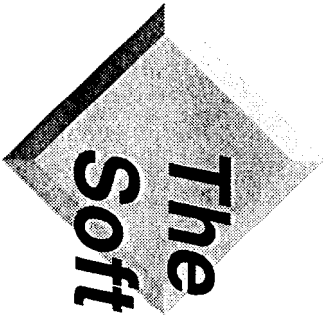
# Measuring Software Evolution by Relative Complexity





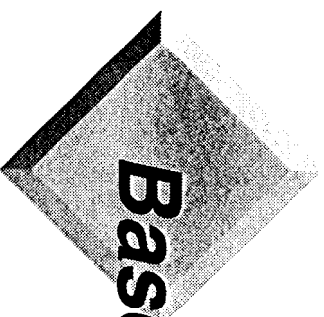
# Measuring Change in Fault Surrogate





# ***The Fault Injection Process During Software Development***

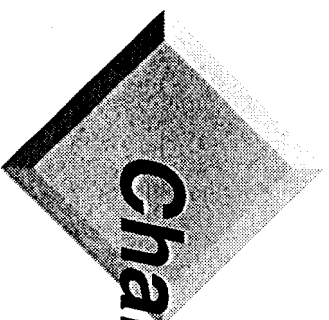
- ❖ Immediately after the first integration test of a software system its complexity will rise in relation to the baseline complexity of the system at the first build
- ❖ The complexity of most software systems will continue to rise over most of the program's useful life
- ❖ We are continually adding functionality to existing software
- ❖ We are continually adding faults to the software in proportion to the complexity of the changes



## ***Baselining Fault Assessment***

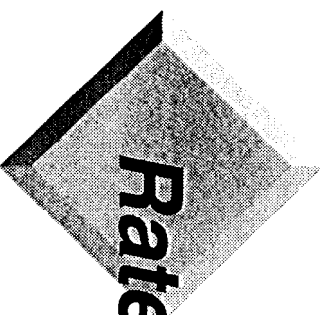
- ❖ Total system complexity is initially  $R = \sum_{i=1}^N p_i$
- ❖ Initially each program module has a number of faults proportional to the fault surrogate
- ❖  $\rho_i^1$  represent the proportion of faults in the  $i^{th}$  module at the first build
- ❖ The fault potential of a module  $i$  is proportional to its value of the relative complexity fault surrogate
- ❖ Thus,

$$r_i = \rho_i / R$$



## Changes to Faults

- ❖ Let  $L^j$  represent the total number of faults found at the  $j^{th}$  build of the system
- ❖ The  $i^{th}$  module will have had  $l_i^j$  faults removed
- ❖ Then  $g_i^j = l_i^j / L_i^j$  represents the proportion of faults removed in the  $i^{th}$  module on the  $j^{th}$  build of the system
- ❖ If the changes to code to fix faults have not changed the fault surrogate measure, then the proportion of faults remaining in the  $i^{th}$  module on the  $j^{th}$  build is  $\delta_i^j = \rho_i - g_i^j$



## *Rate of Fault Injection*

- ❖ New faults will be injected into the system in proportion to the change in the fault surrogate
- ❖ The change relative complexity from build  $j$  to build  $j+1$  is  $\Delta_i^{j+1} = |p_i^j - p_i^{j+1}|$

- ❖ The total change over  $j+1$  builds is

$$s_i^{j+1} = \sum_{k=2}^{j+1} \Delta_i^k$$

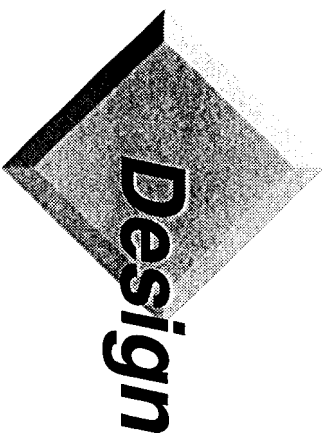
- ❖ New estimate for proportion of remaining faults is

$$\delta_i^{j+1} = s_i^{j+1} - g_i^j$$



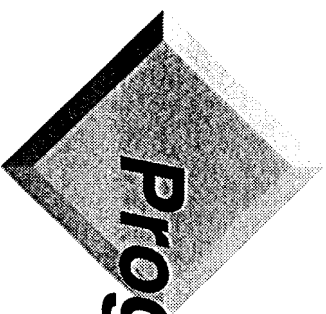
## ***Execution Consequences of Faults: Failures***

- ❖ **A fault can only cause a failure if it is executed**
- ❖ **Different functionalities execute different sets of modules**
- ❖ **Faults can be mapped to program functionalities**



## ASSIG<sup>NS</sup> ( $f,m$ )

| $F \times M$ | $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ |
|--------------|-------|-------|-------|-------|-------|-------|
| $f_1$        | T     | T     |       |       |       |       |
| $f_2$        | T     |       | T     | T     |       |       |
| $f_3$        | T     |       | T     |       |       | T     |
| $f_4$        | T     |       |       | T     |       |       |



## *Program Functionality*

- ❖ Users specify their needs in terms of a set of operations,  $O$
- ❖ Programs implement the operations in a set of functionalities,  $F$
- ❖ The Software Requirements Specifications define a set of relations on  $O \times F$
- ❖ There is a relation **IMPLEMENTS** over  $O \times F$
- ❖ **IMPLEMENTS** ( $o, f$ ) is true if
  - ❖ functionality  $f \in F$  is used to implement
  - ❖ operation  $o \in O$





## IMPLEMENTS ( $o, f$ )

| $O \times F$ | $f_1$ | $f_2$ | $f_3$ | $f_4$ |
|--------------|-------|-------|-------|-------|
| $o_1$        | T     | T     |       |       |
| $o_2$        |       | T     | T     | T     |

Operation  $O_1$  is implemented using functions  $f_1$  and  $f_2$

Operation  $O_2$  is implemented using functions  $f_2$ ,  $f_3$  and  $f_4$



# *Functional Classification of Program Modules*

- ❖ Some program modules **will execute regardless of the functionality**

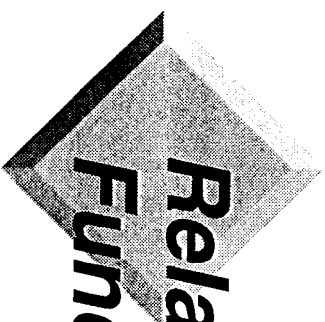
$$M_c = \{m : M \mid \forall f \in F \bullet \text{ASSIGNS } (f, m)\}$$

- ❖ Some program modules are **indispensably associated with a functionality**

$$M_i^{(f)} = \{m : M_f \mid \forall f \in F \bullet \text{ASSIGNS } (f, m) \Rightarrow p(f, m) = 1\}$$

- ❖ Some program modules may **potentially execute when a given function is expressed**

$$M_p^{(f)} = \{m : M_f \mid \exists f \in F \bullet \text{ASSIGNS } (f, m) \wedge 0 < p(f, m) < 1\}$$



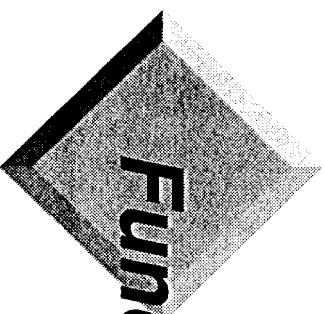
# Relationship of Modules to Functions

| FUNCTION | $M_c$     | $M_i$          | $M_p$          | $M_f$                    |
|----------|-----------|----------------|----------------|--------------------------|
| $f_1$    | $\{m_1\}$ | $\{m_2, m_4\}$ | $\{\}$         | $\{m_1, m_2, m_4\}$      |
| $f_2$    | $\{m_1\}$ | $\{m_3\}$      | $\{m_5\}$      | $\{m_1, m_3, m_5\}$      |
| $f_3$    | $\{m_1\}$ | $\{\}$         | $\{m_3, m_6\}$ | $\{m_1, m_3, m_6\}$      |
| $f_4$    | $\{m_1\}$ | $\{m_3\}$      | $\{m_5, m_6\}$ | $\{m_1, m_3, m_5, m_6\}$ |

where  $M_f = M_c \cup M_p^{(f)} \cup M_i^{(f)}$

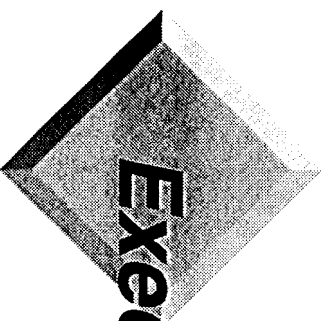


- ❖ The Operational Profile is the set of unconditional probabilities of each of the operations being executed by a user
- ❖ Thus,  $\Pr(O = o_i)$  is the probability that the user is executing an operation  $i$
- ❖ The operations are mutually exclusive
- ❖ The probability distribution of the operational profile is multinomial



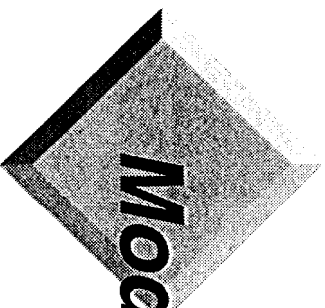
## *Functional Profile*

- ❖ The Functional Profile of the software is the set of unconditional probabilities of each of the functionalities being expressed by an operation
- ❖ Thus  $\Pr(F = f_i)$  is the probability that the system is executing program functionality  $i$
- ❖ The functions are mutually exclusive
- ❖ The probability distribution of the functional profile is multinomial



## ***Execution Profile***

- ❖ An **Execution Profile** is the  $\mathbb{S}$  conditional probability of executing a module  $i$  given a certain functionality  $j$
- ❖ Let  $\vec{r}(M = m_j \mid F = f_i)$  represent this probability for a fixed functionality
- ❖ Underlying distribution is multinomial
- ❖ This distribution is directly determined by the program design
- ❖ We must measure to determine the distribution




## ***Module Profile***

**The Module Profile is the unconditional probability that a module will be executed**

$$\Pr(M_j \cap F_i) = \Pr(M_j F_i) = \Pr(F_i) \Pr(M_j \mid F_i)$$

$$\begin{aligned} \Pr(M_i) &= \sum_j \Pr(M_i F_j) \\ &= \sum_j \Pr(F_j) \Pr(M_i \mid F_j) \end{aligned}$$



## ***Risk Assessment with Fault Surrogate as Loss Function***

- ❖ At each build, an estimate for the proportion of remaining faults is  $\delta_i^j = p_i - g_i^j$
- ❖ Each functionality has a distinct execution profile  $p_i^f$ .
- ❖ The functional risk of this execution profile is

$$\phi^f = \sum_{i=1}^n p_i^f \delta_i^j$$

- ❖ If a functionality is executed that will run fault prone modules with high probability, the risk (failure potential) will be high





## ***Future Work***

- ❖ **Functional standards for fault recording**
- ❖ **Risk Assessment for software test**
- ❖ **New methodology for regression testing based on risk assessment**
- ❖ **New potential for modeling software reliability**